

EUROPEAN CREDIT TRANSFER AND ACCUMULATION SYSTEM (ECTS) pl. M. Skłodowskiej-Curie 5, 60-965 Poznań

# **COURSE DESCRIPTION CARD - SYLLABUS**

Course name			
Elasticity and Plasticity			
Course			
Field of study		Year/Semester	
Building Engineering		1/1	
Area of study (specializa	tion)	Profile of study	
Structural Engineering		general academic	
Level of study		Course offered in	
Second-cycle studies		English	
Form of study		Requirements	
full-time		compulsory	
Number of hours			
Lecture	Laboratory clas	ses Other (e.g. online)	
30	0	0	
Tutorials	Projects/semina	ars	
15	15		
Number of credit points	;		
4			
Lecturers			
Responsible for the course/lecturer:		Responsible for the course/lecturer:	
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Faculty of Civil Engineeri	ng and Transport	Wydział Inżynierii Lądowej i Transportu	
Institute of Building Engi	neering	Instytut Budownictwa	
ul. Piotrowo 5, 60-965 Poznań		ul. Piotrowo 5, 60-965 Poznań	

#### **Prerequisites**

KNOWLEDGE: Basic knowledge of the following subjects: mathematics, theoretical mechanics, strength of materials and structural mechanics covered during Civil Engineering or other similar type of studies up to the Bachelor of Science degree.

SKILLS: Capability to apply the acquired knowledge and obtain further information from the literature. One is capable to apply the theoretical knowledge to solve practical problems.

SOCIAL COMPETENCE: Awareness about necessity of expending the theoretical knowledge in order to justify its application during the professional career. Understanding the necessity of constant education.



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# **Course objective**

The goal of the course is focused on formulating elastic and elasto-plastic constitutive relations for continua. Techniques for solving related boundary value problems will be also covered, including the limit-load method of structural analysis.

## **Course-related learning outcomes**

#### Knowledge

Student knows the concepts of stress and stain tensors, displacement vector in the point of deformable elastic body along with the relations between them.

Student knows the solving methods of two dimensional problems in the field of theory of elasticity.

Student knows the elasto-plastic material models, plasticity conditions and theories describing plastic behaviour.

#### Skills

Student is capable to solve problems involving tensor calculus in absolute, index and matrix notations.

Student is capable to solve 2-D boundary value problems for elastic disks (plane stress and plane strain states).

Student is capable to calculate the ultimate load capacity of bar systems (elasto-plastic beams and frames).

## Social competences

Student is capable to work individually as well as in the team.

Student is aware of the responsibility arising from the accuracy of obtained results and is able to provide the interpretation.

Student is aware of the necessity of constant education and knowledge expansion.

## Methods for verifying learning outcomes and assessment criteria

Learning outcomes presented above are verified as follows:

Written tests and exercises. The lectures will be summerised by written exam.

1) Exam:(two terms: first one during the regular examination period, second during the last chance examination period) - each exam lasts 2 hours - each student receives test with individual and unique problems - the final mark is the summation of all the answers provided to the given problems, passing note in the scale 2= fail, 5= very good can be granted after obtaining at least 50% of the maximum amount of points

2) Tutorial sessions:

- two written tests during semester



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- each student receives the set of two unique problems which must be solved and described individually (projects)

-during the tutoring sessions the individual help will be granted and knowledge of solving problems will be tested

- final grade for each project will be based on the quality of the project as well as the result of the quiz

- dates of each quiz will be set at the beginning of the semester.

## **Programme content**

Elements of tensor calculus. Stress tensor. Analysis of stress state, principal stresses and directions. Equilibrium equations and boundary conditions. Description of movement, Lagrange and Euler coordinates. Analysis of strain state. Strain tensor and its interpretation. Geometrical equations. Constitutive relations, generalized Hooke's law. Principal strains and directions. Lame and Michell's-Beltrami's equations. Energy principles. 2-D stress and strain problems. Airy's stress function. Planar problems in polar coordinates. Boundary value problems and methods of solution. Boussinesq's and Flamant's problems and solutions. Elasto-plastic behaviour of materials. Plastic deformations and plastic flow. Idealized models of elasto-plastic materials. Yield conditions, Tresca and Huber-von Mises criteria. Elasto-plastic bending of beams. Limit load theory and its theorems. Examples of calculation for beams and frames.

## **Teaching methods**

Lecture – traditional lectures ( "chalk-and-talk"), with computer-assisted presentations at times.

Tutorial – discussing and solving problems on the blackboard with plenty of student participation.

Projects – two projects on topics presented at Lectures.

## Bibliography

Basic

- 1. Fung Y. C.: Foundations of solid mechanics, Prentice-Hall, Englewood Cliffs, 1965
- 2. Mase G.E., Theory and problems of continuum mechanics, Mc-Graw Hill , New York 1970
- 3. Ragab A.-R., Bayoumi S.E.: Engineering Solid Mechanics. Fundamentals and Applications, CRC, Boca Raton 1999.
- 4. Skrzypek J., Hetnarski R.B.: Plasticity and creep, CRC Press 1993
- 5. Stein E., Barthold F.-J.: Elastizitätstheorie, Skript, Hannover 2004.
- 6. Mang H.A., Hofstetter G.: Festigkeitslehre, Springer Vieweg 2018

#### Additional

1. Brunarski L., Kwiecinski M.: Wstęp do teorii sprężystości i plastyczności, Wyd. PW, Warszawa 1976.



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- 2. Brunarski L., Górecki B., Runkiewicz L.: Zbiór zadań z teorii sprężystości i plastyczności, Wyd. PW, Warszawa 1976
- 3. Gawęcki A., Mechanika materiałów i konstrukcji prętowych, (tom I+II), Wyd. PP, Poznań 1998
- 4. Krzyś W., Życzkowski M.: Sprężystość i plastyczność, PWN, Warszawa 1962.
- 5. Nowacki W.: Teoria sprężystości, PWN, Warszawa 1970.
- 6. Ostrowska-Maciejewska J., Podstawy mechaniki ośrodków ciągłych, PWN, Warszawa 1982

#### Breakdown of average student's workload

	Hours	ECTS
Total workload	110	4,0
Classes requiring direct contact with the teacher	60	2,0
Student's own work (literature studies, preparation for	50	2,0
laboratory classes/tutorials, preparation for tests/exam, project		
preparation) <sup>1</sup>		

<sup>&</sup>lt;sup>1</sup> delete or add other activities as appropriate